## MATH 402 Worksheet 10

Friday 4/27/18

Review problems
In many constructions, we took a triangle $A B C$, took the midpoints $D, E$ of the sides $A B$ and $A C$ respectively. We then dropped the perpendiculars from $A, B, C$ to the line $D E$ to obtain points $G, F, H$ respectively.
Exercise 1. Verify that $F H B C$ is a Saccheri quadrilateral with base $F H$.
Exercise 2. Show that the triangle $A B C$ and the Saccheri quadrilateral $F H B C$ are equivalent. Keep in mind there are a couple of cases to check. Conclude that the triangle and the Saccheri quadrilateral have the same area.

Exercise 3. Show that if $A B C D$ and $A^{\prime} B^{\prime} C^{\prime} D^{\prime}$ are two Saccheri quadrilaterals with the right angles at $A, B, A^{\prime}, B^{\prime}$ which have the property that the top angles are congruent and $C D \cong C^{\prime} D^{\prime}$, then the Saccheri quadrilaterals are congruent. In particular, show that $A B \cong A^{\prime} B^{\prime}, A C \cong A^{\prime} C^{\prime}$ and $B D \cong B^{\prime} D^{\prime}$.

